



Masonry gravity dams A numerical application for stability analysis

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ABSTRACT:

This work presents a numerical application for stability analysis of masonry gravity dams. From the geometrical dimensions, the material characteristics, hydrostatic loads and seismic loads, the application automatically determines the following results: thrust line for the dead weight load and the dead weight together with the other loads; stress diagram and safety factors for the failure of the dam-foundation contact as part of an overall analysis; safety factors for the failure of horizontal planes along the body of the dam; parametric properties analysis (volumetric mass) and the resistant characteristics (friction angle) on the base of the dam.

The analyses of three historical masonry dams located in Algeria was made. This work highlights the versatility of the numerical application as it can work with different section geometry, including curved and discontinuous sections, and the importance of assessing several scenarios in order to obtain a safe result.

Keywords: *Masonry dams, historical structures, numerical applications, stability analysis*

1 HISTORICAL MASONRY DAMS

The first dams built in 3000 B.C. were constructed of earth and rock, laid out randomly. These dams could close wide valleys but only with small height. As in other fields, the Romans contributed greatly to dam construction. Their ability to manage large projects and the introduction of technical improvements, such as strong hydraulic mortar, are good examples.

The second half of 19th century inaugurates a new era in dam engineering. The works of Sazilly [1], Delocre [2] and Rankine [3] stated design principles for the dam profile. It was a technological evolution in which the economy of material was relevant. Figure 1 compares the section of Puentes dam, constructed between 1785 and 1791, in Spain, and Furens dam, completed in 1866 in France, designed by Delocre. Both of the dams present a stable geometry but the wall volumes differ by about 45%. Only after the collapse of Bouzey dam, in 1895, and the uplift effect begin to be accounted for as an important load. Lévy's [4] paper it has to be pointed out is the most relevant contribution in this direction.

Masonry by definition has a discontinuous nature. To achieve homogeneous behaviour, and on impervious monolith, different construction techniques were developed. Rankine (1872) described the care that must be taken to ensure that every stone shall be "thoroughly and firmly bedded" and to avoid "the practice of grouting" just for filling voids, which should he noted, first filled by stone blocks.

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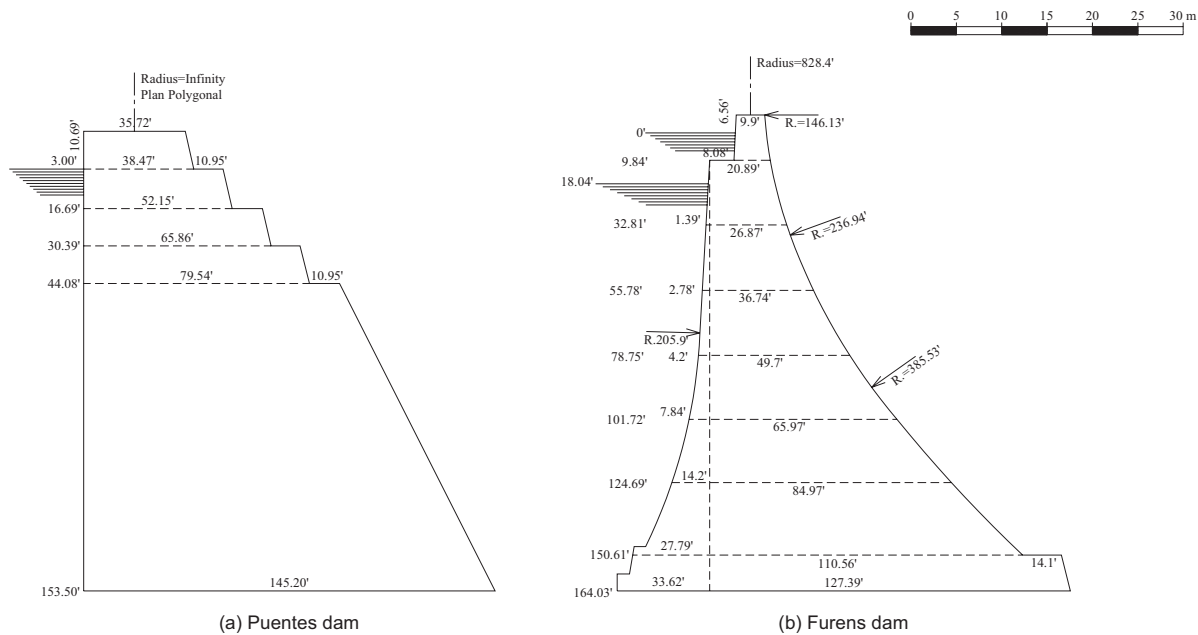


Figure 1. Puentes dam (a) and Furens dam (b) cross sections [after 5]

Masonry used in the construction of dams may be classified as the following types [6, 7]: dimensioned stones, rubble masonry and concrete masonry. The dimensioned stones, comprising of regular well shaped stones, were used for facing and for ornamental propose, as in parapet walls and copings. Rubble masonry was the main material, made with irregular stones, as extracted from the quarry, laid in discontinuous layers and bonded with high quality mortar. The concrete masonry, composed of a mix of Portland cement and broken stones, was applied in the foundation and abutments to fill the voids and seams in the bedrock. The size of the elements assembled in rubble masonry varies. The largest stones, about 25% of the total aggregates, should be less than 0.75m³ and the smallest stones, again about 25% of the total aggregates, should has the size that “two men can lift them”, which means probably 50kg [8].

The construction of La Verdeja dam localized near Avila de los Caballeros, in Spain, was completed in 1901. The dam was torn down in 1989 before being submerged by the reservoir of another dam constructed upstream. The core was made of rubble masonry bonded by hydraulic lime. Portland cement was employed only close to the joints between ashlar, and in the external faces, where high quality stone was used [9].

In the first quarter of 20th century, rubble masonry has been replaced by concrete masonry to a great extent. This could contain a large percentage of large “plums” to allow cement saving. Aspects like fluidity of the concrete and quality of building joints start to arise [10].

Many of these old masonry dams are inspected regularly and safety assessment is an important issue, since the risk is high. Understanding the design assumptions and the construction details underlying their conception helps to evaluate the behaviour and to detect weaknesses. The method presented here is a practical procedure based on the limit analysis of gravity dams.

2 INITIAL ASSUMPTIONS

It is reasonable that safety evaluation of existing structures begins with pragmatic procedures. In the first stage, it is important to identify the phenomena under study and the sensitivity of the main variables. Subsequently, through more sophisticated analyses, which require larger resources and therefore must be focused on the previously identified scenarios, the early results must be confirmed and the safety factors must be determined.

Figure 2 show the loads involved in gravity dams analysis, namely: self weight W ; upstream horizontal ($HP_{h,u}$) and vertical ($HP_{v,u}$) hydrostatic pressures; downstream horizontal ($HP_{h,d}$) and vertical ($HP_{v,d}$) hydrostatic pressures; upstream horizontal ($HPd_{h,u}$) and vertical ($HPd_{v,u}$) hydrodynamic pressures; inertial force of the body of the dam (I_h); and the resultant of the uplift at the base between the upstream face and the drainage gallery ($U_{tot,u-g}$) and between the drainage gallery and the downstream face ($U_{tot,g-d}$).

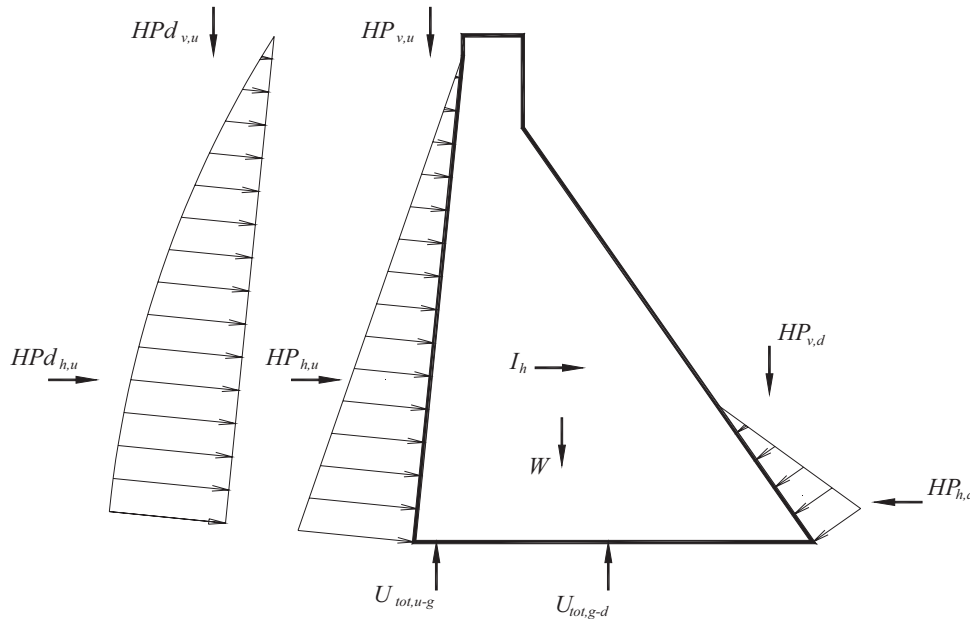


Figure 2. Loads addressed by the numerical application

This is a 2-D plane analysis, therefore applicable to straight gravity dams built in wide valleys. For dams presenting a small in plan curvature, the arch effect is disregarded and the results are conservative, so three-dimensional models may be recommended for a more accurate estimate [11, 12].

Furthermore, this method does not take into account the relative deformability of the dam and foundation. This aspect is important for determining the stress values along the base, in the contact between the dam and the foundation, because actual stresses may be higher, especially when the actions are analyzed independently. If the foundation is highly deformable or if it presents a large heterogeneity, such fact cannot be disregarded since it influences the stresses developed on the body of the dam. The compressive stresses applied to a gravity dam are usually fairly low, and below the material strength for concrete and masonry, and the same can be stated for medium strength foundations, which is why, in this calculation, compressive failure is not considered. This explains why concrete dams use low strength or pozzolanic cements, for economic and practical reasons, and because these cements have lower hydration temperatures than the ones with high strength. On the other hand, the tensile strength is considered zero, which is relevant in the determination of the length of cracks occurring at the base, as well as for the application of the uplift by an iterative procedure.

A Mohr-Coulomb failure model, with zero cohesion, was adopted for the horizontal plane. Therefore, the friction angle is the only shear strength parameter considered. This is justified by the fact that cohesion is difficult to determine by experimental means and has a large scatter. Hence, most international regulations require the use of high partial safety factors, or to disregard it completely. In addition, cohesion only acts in practice when the section is under a minimum

compressive stress, so if this aspect is not observed, it would be unsafe to consider it throughout the entire length of the plane under analysis [13]. Uplift is not considered as an external load, which is why it is not included in the free body diagram. Uplift is locally added to the total vertical stress to obtain effective stresses. If the foundation has a drainage system, the uplift is reduced, leading to a bi-linear uplift diagram, depending on the location of the gallery. A pseudo-static seismic analysis method is adopted, considering the inertial force of the dam and the hydrodynamic effect of water in accordance with Westergaard's solution. It is a simplified method that does not consider the amplification of the value of earthquake acceleration with height and its oscillatory characteristic, using the resultants applied as static loads.

3 NUMERICAL DATA FOR THE MODEL

The calculations are done on a model developed from the idealization of a discrete medium consisting of horizontal elements (Figure 3), which are geometrically represented by the corresponding axes, and defined by the intersections between planes, with upstream and downstream faces. The element thickness (e) may be chosen depending on the dam height. From several analysis done, values of $e = 0.10m$ have been adopted for dams up to 30m height and of $e = 0.50m$ for larger heights.

The required data for the element are: length (L^n); abscissa of the centre (x_c^n); level of the axis (y^n); and abscissa close to the upstream (x_u^n) and downstream (x_d^n) face. Three parameters can be considered independent (x_u^n, x_d^n, y^n), being those introduced to optimize the calculations, with the following relations:

– Length of the element

$$L^n = x_d^n - x_u^n \quad (1)$$

– Abscissa of the centre of the element

$$x_c^n = \frac{x_u^n + x_d^n}{2} \quad (2)$$

The loads presented in Figure 2 are considered, at the level of element n , as follows (Figure 4):

– Self weight

$$W^n = L^n e \gamma^{mat} \quad (3)$$

– Upstream horizontal hydrostatic pressure

$$HP_{h,u}^n = (z_{HP,u} - y^n) \gamma^w e \Leftrightarrow z_{HP,u} \geq y^n \quad (4)$$

– Upstream vertical hydrostatic pressure

$$HP_{v,u}^n = (z_{HP,u} - y^n) \gamma^w (x_u^n - x_u^{n+1}) \Leftrightarrow z_{HP,u} \geq y^n \quad (5)$$

– Downstream horizontal hydrostatic pressure

$$HP_{h,d}^n = (z_{HP,d} - y^n) \gamma^w e \Leftrightarrow z_{HP,d} \geq y^n \quad (6)$$

– Downstream vertical hydrostatic pressure

$$HP_{v,d}^n = (z_{HP,d} - y^n) \gamma^w (x_d^{n+1} - x_d^n) \Leftrightarrow z_{HP,d} \geq y^n \quad (7)$$

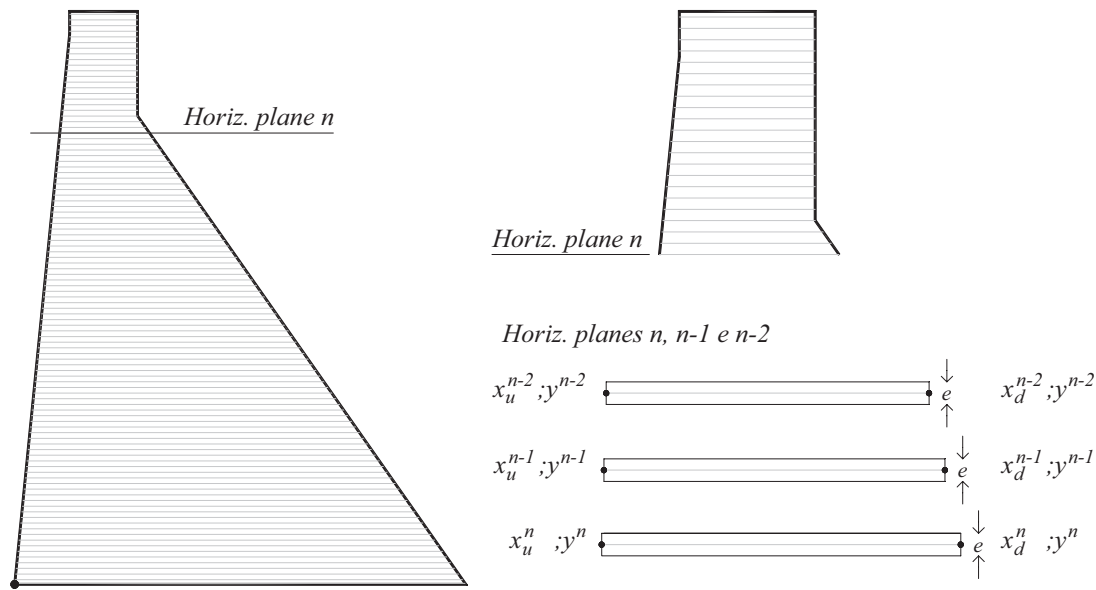


Figure 3. Discretization scheme of the dam body

– Upstream horizontal hydrodynamic pressure (Westergaard’s solution)

$$HP_{h,u}^n = \frac{7}{8} a_h \gamma^w \sqrt{(z_{HP,u} - y_{found})(z_{HP,u} - y^n)} e \Leftrightarrow z_{HP,u} \geq y^n \quad (8)$$

– Upstream vertical hydrodynamic pressure

$$HP_{v,u}^n = \frac{7}{8} a_h \gamma^w \sqrt{(z_{HP,u} - y_{found})(z_{HP,u} - y^n)} (x_u^n - x_u^{n+1}) \Leftrightarrow z_{HP,u} \geq y^n \quad (9)$$

– Inertial load

$$I_h^n = L_n e \gamma^{mat} a_h \quad (10)$$

Here, γ^{mat} is the volumetric weight of the material, γ^w is the volumetric weight of water, $z_{HP,u}$ is the upstream water level, $z_{HP,d}$ is the downstream water level, y_{found} is the foundation level and a_h is the seismic coefficient in the horizontal direction

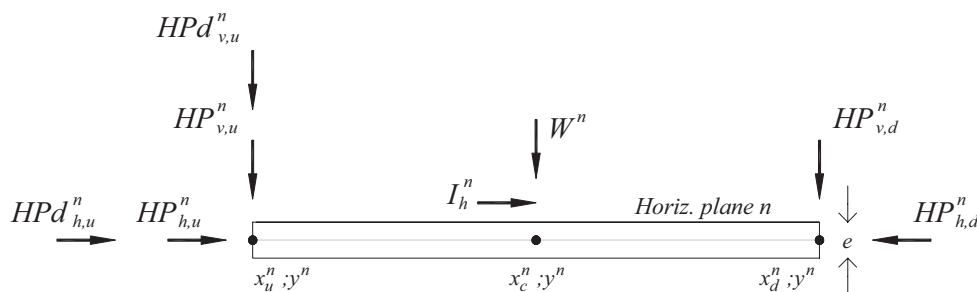


Figure 4. Load representation in single element

The hydrostatic and the hydrodynamic pressures acting on the face of an element are assumed to have a rectangular distribution, which is an acceptable approximation for small thickness elements

(e). For a given horizontal plane, the analysis is undertaken by integrating the elements (e) placed above the plane. The smaller the thickness adopted, the higher the accuracy of results, i.e., by taking the self weight as an example, the following holds:

$$\lim_{e \rightarrow 0} \left| \sum W^n - W \right| \rightarrow 0 \quad (11)$$

4 DETERMINATION OF RESULTS

The application makes it possible to visualize on a graph the thrust lines due to the action of self weight, corresponding to the situation of an empty reservoir, and to the combined action of self weight with other actions. The concept of thrust line results from the graphic statics, corresponds to the geometrical place occupied by the static resultant in each horizontal plane of loads applied above that plane. It has an important physical meaning, because it represents the load distribution across the body of the structure. Through its observation, it is possible to identify tensile zones, which occur in these planes in which the thrust line is outside the middle third of the section. Furthermore, it is also possible to observe on a graph the total and effective vertical stresses. The total stresses are obtained in the following way:

$$\sigma = \frac{\sum V}{A} \pm \frac{\sum M}{I} y, \quad (12)$$

in which,

σ – Total vertical stress;

$\sum V$ – Sum of the vertical component of actions (except for uplift, which was not considered as an external action);

$\sum M$ – Sum of moments due to actions;

A – Area of the base (per meter of the dam length);

I – Inertial moment of the plane (per meter of the dam length);

y – Distance to the downstream and upstream faces.

The effective stresses are determined from total stresses by adding the uplift pressure. Generally, the uplift diagram presents a bi-linear configuration (Figure 5a), resulting from the triangular diagram and from the effect of the reduction in the drainage system. The diagram can be updated whenever a new crack arises, close to the upstream face, where the full uplift is applied (Figure 5b) [14], leading to the iterative calculation of the final length of the crack. The initial length of the crack, for a previously defined load scenario, is determined on the basis of the criterion of zero tensile resistance. The calculation of the final length of the crack takes into account the assumptions as follows:

- After the occurrence of the initial crack, it is considered that the drainage system loses its effectiveness (other less conservative hypotheses would be admissible, such as considering the loss of effectiveness of the drainage system only in the cases when the crack was developed beyond the zone of installation of the drains), and, therefore, the pressure diagram acquires a rectangular configuration along the crack and a trapezoidal or triangular configuration, depending on the downstream water level, along the non-cracked surface;
- Unlike the previously adopted strategy, the uplift becomes part of the eccentricity and stress calculations; otherwise it would not be possible to establish an iterative calculation method to simulate the progression of the crack.

The factor of safety to sliding (SSF), in any horizontal plane, including the base, for the actions applied above their level, is given by:

$$SSF = \frac{(\sum V) \tan \phi}{\sum H}, \quad (13)$$

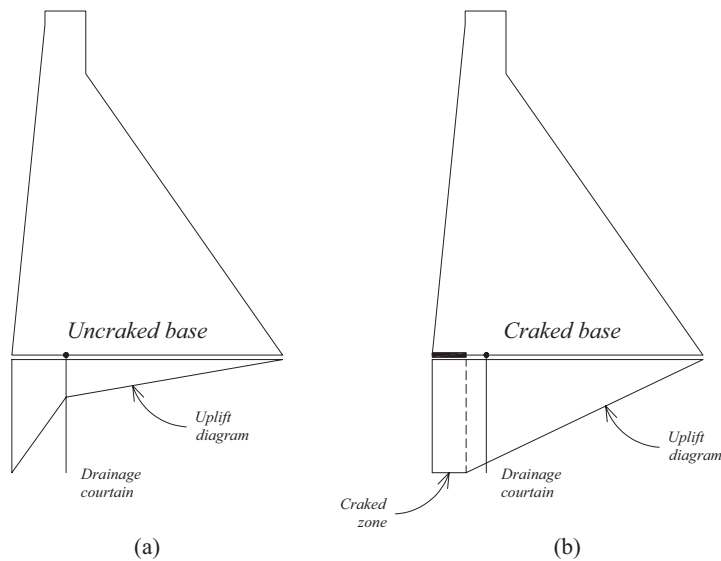


Figure 5. Uplift diagram for uncracked base (a) and cracked base (b)

in which $\sum V$ is the sum of the vertical component of actions (including the uplift. In this case, the effect of uplift can be physically interpreted as a reduction in self weight [15]), $\tan \phi$ is the tangent of the friction angle and $\sum H$ is the sum of the horizontal component of actions.

The overturning safety factor (OSF) is given by:

$$OSF = \frac{\sum M_{sta}}{\sum M_{ope}},$$

in which $\sum M_{sta}$ is the sum of stabilizing moments and $\sum M_{ope}$ is the sum of applied moments.

For the analysis throughout the body of the dam, at the various horizontal planes defined as the thickness (e), the full uplift is considered for each of these levels, without any reduction factor, because it is assumed that there is no vertical drainage system installed on the body of the dam. The other actions reflect the load cases adopted.

The available parametric analysis, for the self weight and the friction angle, refer to the horizontal plane of contact between the dam and the foundation and to the load cases considered, according to the hypotheses admitted for the uplift.

5 THREE MASONRY DAMS IN ALGERIA

At the end of the 19th century the French government was involved in the construction of several masonry dams in Algeria for irrigation and water supply. Three of them, Gran Cheurfas (Figure 6a), 39.9m of height, finished in 1884 and which failed in 1885, Habra (Figure 6b) , 38.1m of height, finished in 1871 and failed in 1881, and Hamiz dam (Figure 6c) , 38.1m of height, finished in 1885, are worthy of special attention since they collapsed. In fact, they were designed before the Bouzey dam accident and were not designed to withstand the uplift pressure. As in other examples this aspect plays a key role in dam behaviour and the collapse mechanism.

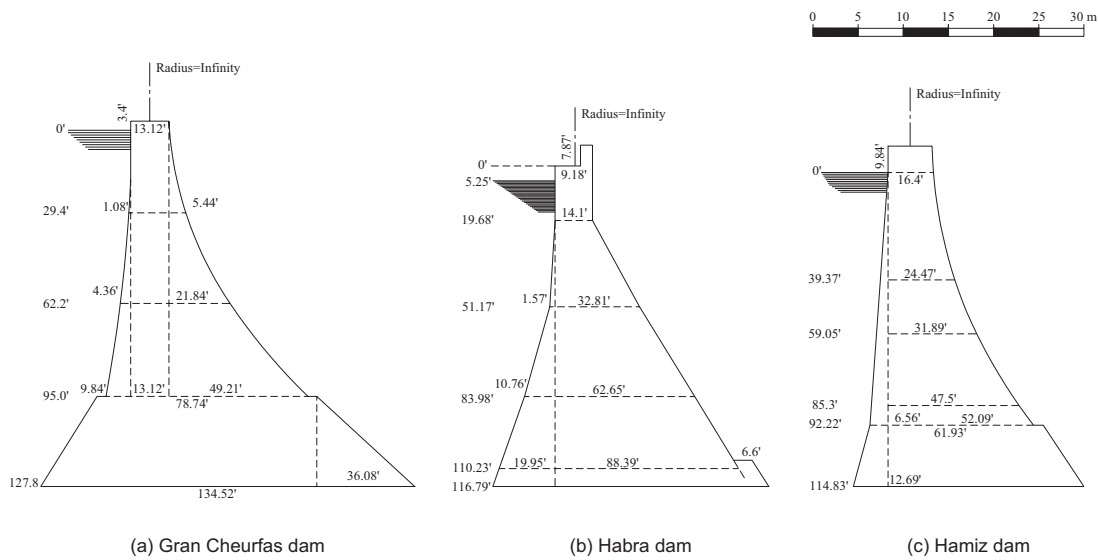


Figure 6. Cross sections of Gran Cheurfas (a), Habra (b) and Hamiz (c) dam [after 5]

In the case of Gran Cheurfas dam and Hamiz dam information about the collapse is limited. Based on the analyses developed for Gran Cheurfas dam (Figure 7) and Hamiz dam (Figure 8), it is possible to conclude that collapses were triggered by crack propagation near the foundation, followed by an uplift increase. The rupture of Habra dam is more documented since it cost 209 lives. According to Smith [16], Habra’s collapse could have been predicted if the technical and scientific community had paid attention to the Bouzey accident. Wegmann [6] described that the Habra dam ruptured after an “unusually severe storm” which “caused a large wave whose height can be calculates as about 1m”. Figure 9 plots the results for the two following conditions: operating level (OL) and flood level (FL). For flood level, the crack development process was computed with an initial length of 9.7m (tensile stress zone). With no tensile strength and full uplift, the section is not stable.

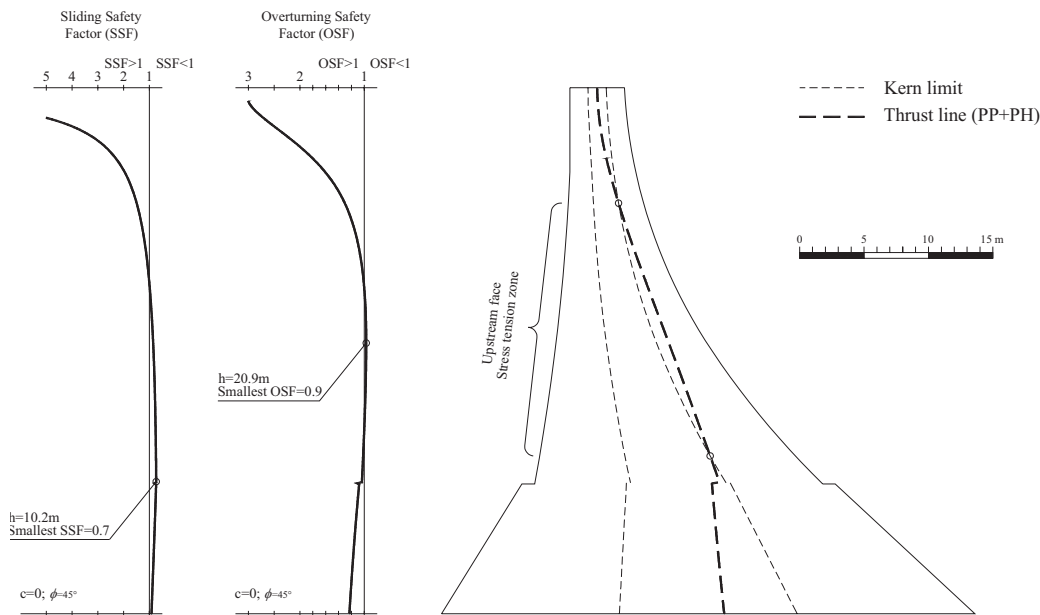


Figure 7. Gran Cheurfas dam analysis

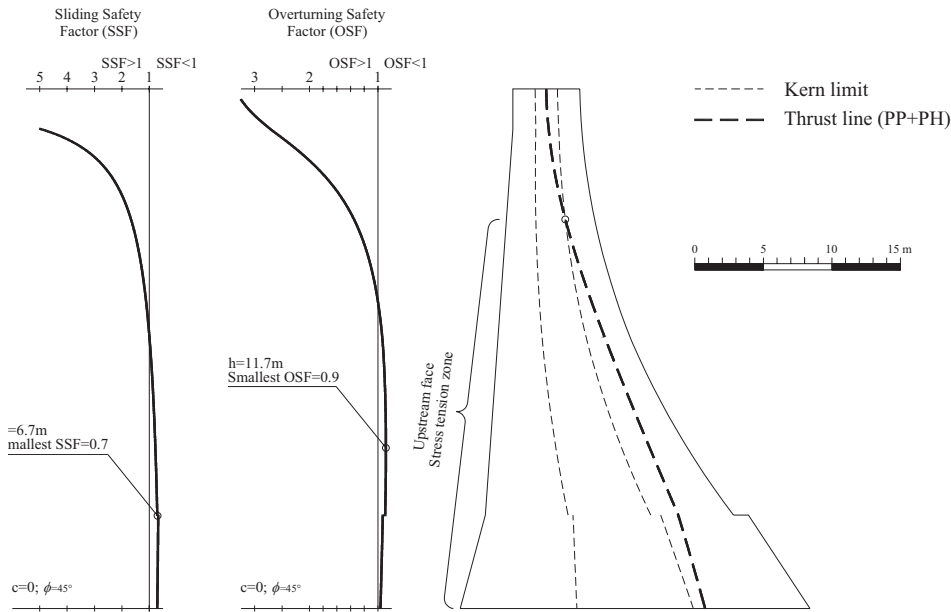


Figure 8. Hamiz dam analysis

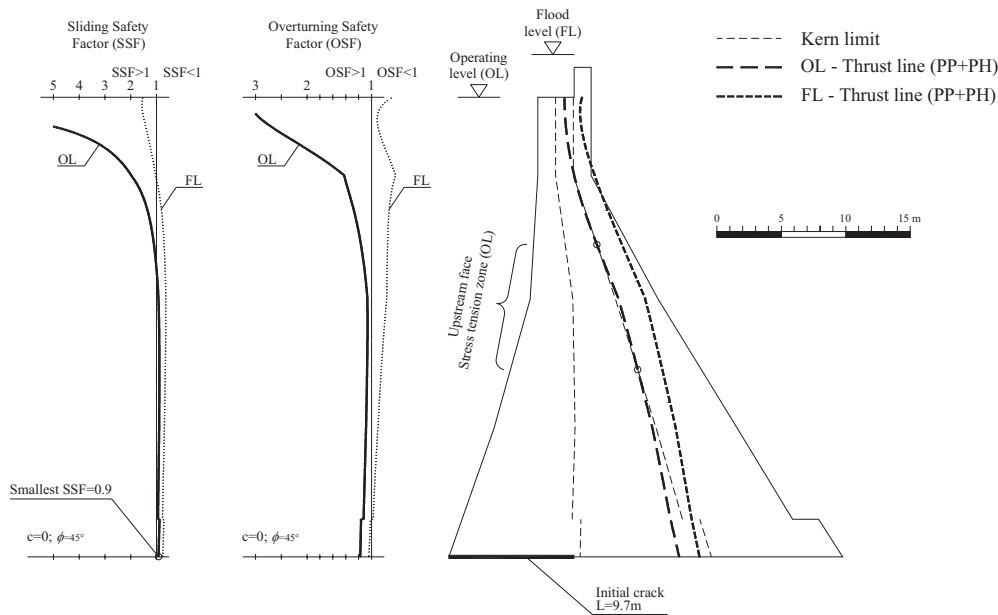


Figure 9. Habra dam analysis

6 CONCLUSIONS

An application developed for the pragmatic assessment of the safety conditions of gravity dams was presented. It has much flexibility, as profiles of different geometry, including curved faces and discontinuities, can be studied. Several examples of such profiles have been presented.

From the results computed for the case studies, dams for which uplift was not considered in their design are likely not to satisfy the safety conditions prescribed by current regulations. In many cases, this fact motivated the execution of rehabilitation works and three collapses in Algeria were discussed.

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