## Immobilised Particles in Gel Matrix-Type Porous Media. Homogeneous porous media model

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Diffusion in pure gels and gels with immobilised cells were analysed. A model of diffusion in immobilised cell gel assuming of homogeneous cells distribution in gel was improved by introducing a tortuosity value. By theoretical analysis and numerical modelling it was shown that tortuosity of a gel with immobilised cells is the result of two factors: 1) a tortuosity generated by cells,  $T_c$ , and 2) a tortuosity of the gel matrix,  $T_g$ . Both variables are function of cell volume fraction,  $\phi_c$ . Hence, the total path length in the gel with immobilised cell is  $L_{\Sigma} = T_c T_g L$  and total tortuosity will be  $T_{\Sigma} = L_{\Sigma} / L = T_c \cdot T_g$ .

Based on this approach it is possible to analyse the data for a gel + cells system, where in general tortuosity seems too large. It is shown in this work that the diffusivity  $\eta = D_e / D_0$  for this system is a complex function of: 1) diffusivity in gel,  $\eta_g$  and 2) diffusivity in immobilised cells,  $\mathfrak{m}_c$ . Hence

$$\eta_c = D_e / D_g$$
, or  $D_e = \eta_c D_g$ , and  $D_e / D_0 = \eta_c \frac{D_g}{D_0} = \eta_c \eta_g$ , where  $D_g$  is the diffusion coefficient

in pure gel matrix, and  $D_0$  is the diffusion coefficient in bulk liquid. Diffusion in a pure gel without immobilised cells is represented by the equation  $\eta_g = D_g / D_0 = \varepsilon_g / T_g$ , where  $M_g$  is the gel porosity, and  $T_g$  is the pure gel tortuosity (average ratio of molecule path to porous media thickness).

The total diffusivity, with tortuosity  $T_c$  and  $T_g$  depending on volume fraction of immobilised

cells 
$$(1 - \phi_c) = \varepsilon_c$$
, is  $\eta = \eta_g \eta_c = \frac{\varepsilon_g}{T_g} \cdot \frac{\varepsilon_c}{T_c(\varepsilon_c) \cdot T_g(\varepsilon_c)}$ .

For the general case, the tortuosity created in the matrix by cells presence is  $T_c(\varepsilon_c) = 1/\varepsilon_c^{\beta} = 1/(1-\phi_c)^{\beta}$  and the tortuosity of gel matrix filled with cells is  $T_g(\varepsilon) = 1/\varepsilon_c^{\gamma} = 1/(1-\phi_c)^{\gamma}$ . Thus:  $D_e/D_0 = \eta_g \cdot (1-\phi_c) \cdot (1-\phi_c)^{\beta} (1-\phi_c)^{\gamma} = \eta_g (1-\phi_c)^{\alpha}$ , and  $\alpha = 1 + \beta + \gamma$ , where  $\beta$  and  $\gamma$  are order values in the range from 0 to 1, and  $\mathfrak{m}_g$  is the ratio  $D_g/D_0$  for pure gels. In the particular case when  $T_g(\varepsilon_c) = T_c(\varepsilon_c) = T$ , and  $T \sim 1/\sqrt{\varepsilon_c}$  the equation

becomes 
$$\eta = \frac{D_e}{D_0} = \frac{\varepsilon_g}{T_g} \cdot \frac{\varepsilon_c}{T^2} = \eta_g \varepsilon_c^2$$

The developed model gave the possibility to describe the dependence of  $D_e/D_0$  on  $\phi_c$ . Comparison with numerous published experimental data showed a good approach. Not all experimental data could be fitted with this homogeneous model. These deviations case might be explained by non-homogeneous cell distributions inside the gel matrix.